

## **International Permit Trading: Efficiency and Transfers**

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2001

This note is a draft of Appendix A of McKibbin, Warwick J. and Peter J. Wilcoxon (2002), *Climate Change Policy after Kyoto: Blueprint for a Realistic Approach*, Washington: The Brookings Institution.

Allowing emissions permits to be traded internationally can improve economic efficiency but it can also lead to large international transfers of wealth. Unfortunately, these features go hand in hand: the conditions under which international trading is most important for efficiency are also the ones that lead to the largest transfers. Since large international transfers will reduce the political viability of a proposed policy, and even the *potential* for large transfers is likely to have a chilling effect, it is important to investigate whether the efficiency gains from trading are large enough to be worth the political and administrative problems trading would create. One way to approach this is to calculate how large the gains from trade are relative to the transfers involved. In this appendix we present a simple economic model that can be used to explore that question.

Suppose that a group of countries would like to lower its greenhouse gas emissions by  $Q^*$  tons, and that the marginal cost of abatement for country  $i$  depends on the amount of abatement,  $q_i$  it does:  $mc_i(q_i)$ . Pareto efficiency requires that the allocation of abatement across countries be such that marginal costs are equal between all pairs of countries,  $i$  and  $j$ :

$$(1) \quad mc_i(q_i^*) = mc_j(q_j^*)$$

where  $q_i^*$  and  $q_j^*$  are the efficient quantities of abatement in the two countries. In addition, total abatement must add up to  $Q^*$ :

$$(2) \quad \sum_i q_i^* = Q^*$$

For convenience, let the marginal cost under the efficient allocation of abatement be denoted by  $A$ :

$$(3) \quad A = mc_i(q_i^*) = mc_j(q_j^*)$$

Now suppose that the marginal cost of eliminating a ton of emissions for country  $i$  when abatement is  $q_i$  can be written as follows:

$$(4) \quad mc_i = A \left( \frac{q_i}{q_i^*} \right)^{\eta_i}$$

where  $\eta_i$  is an elasticity reflecting the rate at which marginal costs increase as abatement departs from its efficient level. When abatement is allocated efficiently,  $q_i$  is equal to  $q_i^*$  and  $mc_i$  will equal  $A$ . A one percent increase in  $q_i$  above  $q_i^*$  will raise marginal costs by approximately  $\eta_i$  percent.

Integrating (4) gives the total cost to country  $i$  of abating  $q_i$  units:

$$(5) \quad tc_i = \frac{A}{1 + \eta_i} \left( \frac{q_i}{q_i^*} \right)^{\eta_i} q_i$$

At the efficient allocation of abatement across countries,  $q_i = q_i^*$  and (5) can be rewritten:

$$(6) \quad tc_i^* = \frac{Aq_i^*}{1 + \eta_i}$$

When the cost elasticity  $\eta_i$  is very small, marginal abatement costs are nearly constant at  $A$  and  $tc_i$  is close to  $Aq_i^*$ . When  $\eta_i$  is larger, the total cost of  $q_i^*$  declines (holding the marginal cost of  $q_i^*$  constant at  $A$ ) because inframarginal units are cheaper to abate. Put another way, a larger  $\eta_i$  means a steeper marginal cost curve, and hence a sharper

reduction in marginal costs when  $q_i$  is below  $q_i^*$ . When  $\eta_i$  is 1.0, for example,  $tc_i$  drops to half of  $Aq_i^*$ .

Now suppose that non-tradable emissions permits are handed out and that country  $i$ 's allotment requires it to do an amount of abatement that differs from the efficient pattern by a percentage  $\varepsilon_i$ :

$$(7) \quad q_i = q_i^* (1 + \varepsilon_i)$$

The sum of the  $\varepsilon_i$ 's across countries will be equal to zero.<sup>1</sup>  $\varepsilon_i$  will be positive when country  $i$  has been given relatively few permits and therefore must abate more than its efficient amount; it will be negative in the opposite case. Because  $q_i$  differs from  $q_i^*$ , marginal costs will no longer be equal across countries. Inserting (7) into (4):

$$(8) \quad mc_i = A(1 + \varepsilon_i)^{\eta_i}$$

Total abatement costs in each country will differ from their efficient values as well, as can be seen by inserting (7) into (5), collecting terms, and then using (6) to write the actual costs in terms of the efficient value:

$$(9) \quad tc_i^N = tc_i^* (1 + \varepsilon_i)^{1+\eta_i}$$

In contrast, if the permits were internationally tradable in a competitive market, the equilibrium price of a one-ton permit would be  $A$  and country  $i$  would buy  $\varepsilon_i q_i^*$  permits from abroad (or sell permits, when  $\varepsilon_i$  is negative) at a total expenditure given by:

$$(10) \quad tc_i^P = \varepsilon_i q_i^* A$$

Using (6) allows this to be rewritten in terms of efficient total costs:

$$(11) \quad tc_i^P = \varepsilon_i tc_i^* (1 + \eta_i)$$

This would allow it to move its level of abatement to  $q_i^*$ , and its total cost – including both abatement and permit purchases or sales – would become:

$$(12) \quad tc_i^T = tc_i^* + tc_i^P$$

Inserting (11):

$$(13) \quad tc_i^T = tc_i^* (1 + \varepsilon_i + \varepsilon_i \eta_i)$$

Now define  $g_i$  be the cost advantage of trading:

$$(14) \quad g_i = tc_i^N - tc_i^T = tc_i^* ((1 + \varepsilon_i)^{1+\eta_i} - 1 - \varepsilon_i - \varepsilon_i \eta_i)$$

When  $\varepsilon_i$  is zero,  $g_i$  is equal to zero: if abatement is allocated efficiently across countries, there will be no need for trading and costs will be the same whether or not trading is allowed. Moving  $\varepsilon_i$  away from zero in either direction raises  $g_i$ , which can be seen differentiating (14) with respect to  $\varepsilon_i$ :

$$(15) \quad \frac{dg_i}{d\varepsilon_i} = tc_i^* (1 + \eta_i) ((1 + \varepsilon_i)^{\eta_i} - 1)$$

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<sup>1</sup> This means that the overall amount of abatement will be correct, just not its allocation across countries.

The derivative will have the same sign as  $\varepsilon_i$ , so moving  $\varepsilon_i$  away from zero in either direction raises the cost advantage of trading.<sup>2</sup> All countries, in other words, will be at least as well off under trading: those with  $\varepsilon_i = 0$  will be no worse off and all others will be strictly better off.

What we have shown so far is a result that is very familiar to most economists: allowing emissions permits to be traded can reduce overall abatement costs and will be weakly preferred by all agents to a non-tradable system. That statement, however, is purely qualitative and gives no indication about whether the gains are small or large. Moreover, it ignores any administrative or political costs that trading might create. As a result, it is not useful for real-world policy decisions: a trading policy that produced small gains from trade at the cost of large administrative or political problems would be inefficient and counterproductive overall.

One way to move beyond a purely qualitative result is to compare the gains from trade to the value of the international permit transactions necessary to bring them about, since the latter is likely to be closely correlated with the political costs of the policy. Let  $\phi_i$  be the ratio between the two:

$$(16) \quad \phi_i = \frac{g_i}{tc_i^P} = \frac{(1 + \varepsilon_i)^{1+\eta_i} - 1 - \varepsilon_i - \varepsilon_i \eta_i}{\varepsilon_i(1 + \eta_i)}$$

Simplifying this slightly gives:

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<sup>2</sup> This equation holds when  $\varepsilon_i$  is greater than  $-1$ ; if  $\varepsilon_i$  were less than  $-1$  (a country were given more than 100 percent of the emissions rights it needed), trading would still be superior but the derivation would be slightly different because total costs in the no-trading case would be zero.

$$(17) \quad \phi_i = \frac{(1 + \varepsilon_i)^{1+\eta_i} - 1}{\varepsilon_i(1 + \eta_i)} - 1$$

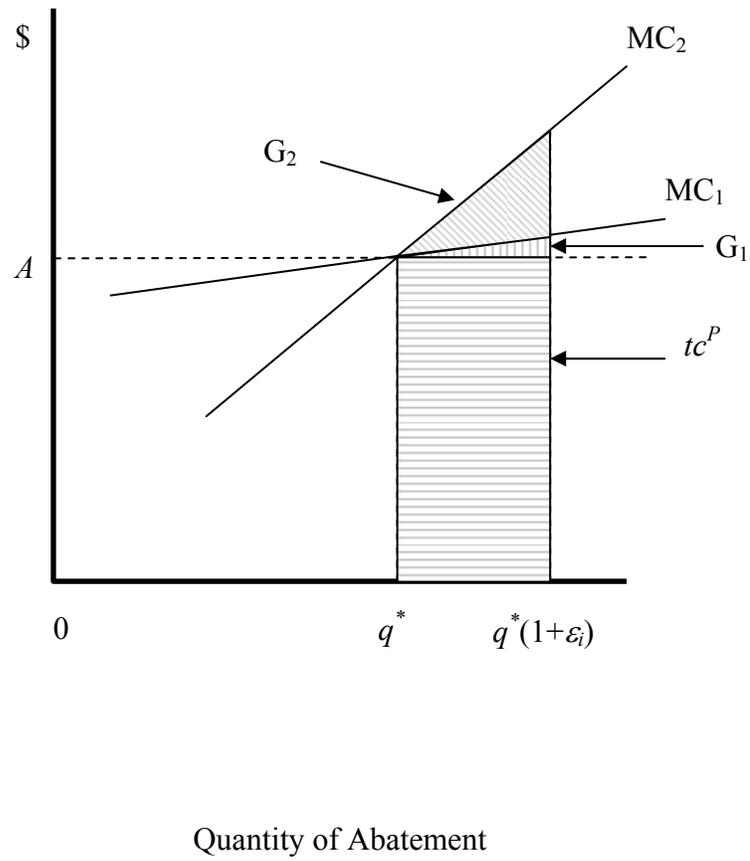
When  $\phi_i$  is large, trading is likely to be a sound, practical policy: the gains from trade are large compared to the transfers it would cause. On the other hand, when  $\phi_i$  is small, it may be that the gains from trade will be overwhelmed by the political costs.

From (17) it is clear that as either  $\varepsilon_i$  or  $\eta_i$  approaches zero,  $\phi_i$  approaches zero as well. The intuition behind this is straightforward and can be seen from Figure 1, which illustrates the relationship between  $\eta$ , marginal costs,  $\varepsilon$  and  $tc^P$ . Suppose a country is initially allocated fewer than the efficient number of permits and would have to abate  $q^*(1+\varepsilon)$  tons. If the elasticity of marginal abatement costs,  $\eta$ , were small, it would face a cost curve like  $MC_1$ . By buying permits at a total cost shown by area  $tc^P$  in the diagram, the country would lower abatement costs enough to produce a net gain equal to area  $G_1$ . The net gain is positive but small compared to  $tc^P$  because the marginal cost curve is fairly flat. The ratio is larger when the marginal cost curve is steeper: a larger  $\eta$  would lead to a cost curve like  $MC_2$  and a gain of  $G_2$ .

The analysis can be taken one step further by evaluating (17) for a range of values of  $\eta_i$  and  $\varepsilon_i$ . The results are shown in Table 1. If the cost elasticity,  $\eta_i$ , is very high and the permits are allocated very inefficiently ( $\varepsilon_i$  is large), the efficiency gain will be relatively large compared to the transfer. For example, when  $\eta_i = 4$  and  $\varepsilon_i = 0.30$ ,  $\phi_i$  will be about 81 percent. However, if either or both of these parameters are small, the gains from trade will be small compared to the transfer. All of the cells above the gray region, in particular, have gains from trade that are less than 10 percent of the permit

transactions. Put another way, in this region the value of permit sales will be more than 10 times the efficiency gains they create.

**Figure 1: Efficiency Gains and Transfers For Different Values of  $\eta$**



**Table 1: Ratio  $\phi$  for Alternative Values of  $\eta$  and  $\varepsilon$**

		<b>Excess Abatement, <math>\varepsilon</math></b>					
		0.05	0.10	0.15	0.20	0.25	0.30
<b>MC elasticity, <math>\eta</math></b>	0.25	0.62%	1.22%	1.81%	2.38%	2.95%	3.50%
	0.50	1.24%	2.46%	3.66%	4.84%	6.01%	7.16%
	0.75	1.87%	3.72%	5.56%	7.38%	9.19%	10.99%
	1.00	2.50%	5.00%	7.50%	10.00%	12.50%	15.00%
	1.50	3.78%	7.62%	11.53%	15.49%	19.51%	23.59%
	2.00	5.08%	10.33%	15.75%	21.33%	27.08%	33.00%
	3.00	7.75%	16.03%	24.83%	34.20%	44.14%	54.68%
	4.00	10.51%	22.10%	34.85%	48.83%	64.14%	80.86%