# E: Efficient incentive design, part 2

## Summary of the principal-agent (PA) version of the biofuels startup

## Participants:

Founder (F): Has **idea** but no cash

Venture capitalist (VC): Has cash but no idea

## Payoffs:

Success (S): \$1M

Failure (F): \$10k

No startup (N): \$100k

Founder's effort (E) affects chance of success (S) but is costly to F:

Level of effort	Cost to F	Prob of S
High (H):	\$5k	20%
Low (L):	\$2k	15%

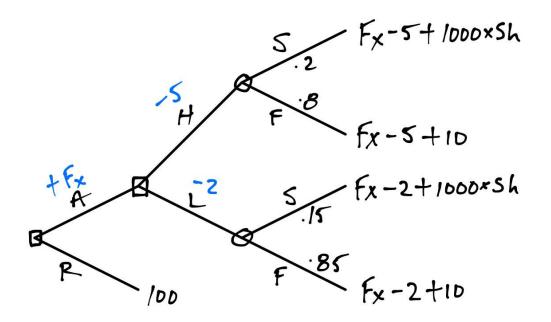
# Case 2: Designing a contract that works

#### Two parameters:

Fixed payment (**Fx**) VC pays to founder

Share of ownership (**Sh**) Retained by founder

Founder's tree with **Fx** and **Sh** variables:



F's payoffs from effort choice, in thousands:

$$EV_H = 0.2 * (Fx - 5 + 1000 * Sh) + 0.8 * (Fx - 5 + 10)$$
  
$$EV_H = Fx + 200 * Sh + 3$$

$$EV_L = 0.15 * (Fx - 2 + 1000 * Sh) + 0.85 * (Fx - 2 + 10)$$

$$EV_L = Fx + 150 * Sh + 6.5$$

$$EV_N = 100$$

IC: What's required for incentive compatibility?

• Want F to choose H: need  $EV_H > EV_L$ 

$$Fx + 200 * Sh + 3 > Fx + 150 * Sh + 6.5$$

$$200 * Sh + 3 > 150 * Sh + 6.5$$

$$50 * Sh > 3.5$$

$$Sh > \frac{3.5}{50}$$

Conclusion: Sh > 7%

Need at least 7% ownership to have enough skin in the game

PC: What's required for participation?

• Want payoff from H to beat salary: need  $EV_H > EV_N$ 

$$Fx + 200 * Sh + 3 > 100$$

$$Fx > 97 - 200 * Sh$$

One possible offer:

VC chooses: Sh = 10%

$$Fx > 97 - 200 * 0.1$$

Viable offer: Fx = 80

Does it work for the founder?

$$EV_H = 80 + 200 * (0.1) + 3 = 103$$

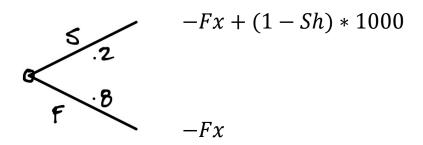
$$EV_L = 80 + 150 * (0.1) + 6.5 = 101.5$$

• Passes IC test:  $EV_H > EV_L$ 

$$EV_N = 100$$

- Passes PC test:  $EV_H > EV_N$
- Net gain: 103 100 = 3

Is it OK for the VC?



General EV:

$$EV_V = 0.2 * (-Fx + (1 - Sh) * 1000) + 0.8 * (-Fx)$$

$$EV_V = -Fx + 200 * (1 - Sh)$$

#### This offer:

$$EV_V = -80 + 200 * 0.9$$

$$EV_V = -80 + 180 = 100$$

• Positive for the VC

## Overall payoff:

Founder: 3k

VC: 100k

Total: 103k

What happened to the other 5k?

## Generalizing to find range of viable contracts:

#### Founder:

IC: 
$$EV_H > EV_L$$
  $Sh > 7\%$ 

PC: 
$$EV_H > EV_N$$
  $Fx > 97 - 200 * Sh$ 

VC:

VC: 
$$EV_V > 0$$
  $200 * (1 - Sh) > Fx$ 

### Graphing:

Sh on Y, Fx on X

## Intercepts:

IC: 
$$Sh > 7\%$$

Y:7%

X:na

Also, higher Sh is better

PC: 
$$Fx > 97 - 200 * Sh$$

$$X : Sh = 0, Fx = 97$$

Y: Fx = 0, Sh = 48.5%

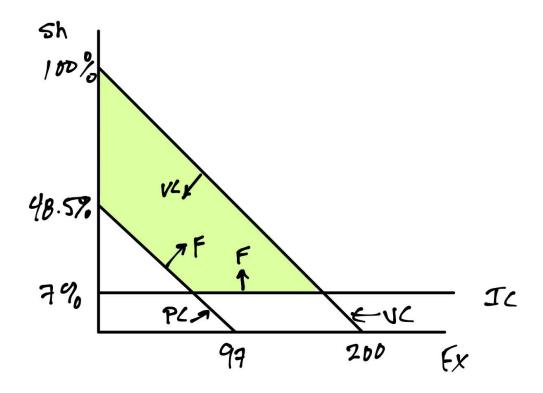
Also, higher Fx or Sh is better

$$VC: 200 * (1 - Sh) > Fx$$

$$X : Sh = 0, Fx = 200$$

$$Y : Fx = 0, Sh = 100\%$$

Also, lower Sh or Fx is better



For reference: intersection of IC, PC

$$Sh = 7\%, Fx = 83k$$